

# EXAM FM QUESTIONS OF THE WEEK

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## Week of August 13/07

An investment fund begins and ends the year with a balance of 100.

A deposit of 10 is made at time  $s$  and withdrawal of 20 is made at time  $s + \frac{1}{2}$ , where  $0 < s < \frac{1}{2}$ . Find the maximum and minimum possible dollar-weighted returns that can occur.

**The solution can be found below.**

## **Week of August 13/07 - Solution**

The dollar-weighted return is  $i$  in the equation

$$100(1 + i) + 10[1 + (1 - s)i] - 20[1 + (1 - s - \frac{1}{2})i] = 100 .$$

Solving for  $i$  results in  $i = \frac{10}{100+10(1-s)-20(1-s-\frac{1}{2})} = \frac{10}{100+10s} .$

Since  $0 < s < \frac{1}{2}$ , it follows that  $0 < 10s < 5$ ,

and then  $100 < 100 + 10s < 105$ , and then  $\frac{10}{105} < \frac{10}{100+10s} < \frac{10}{100} .$

The minimum and maximum values of  $i$  are  $\frac{10}{105} = .0952$  and  $\frac{10}{100} = .10$  .